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Research Paper

Modeling the Effectiveness of Hollow Fiber Membrane Contactors for CO₂ Capture Using Ionic Liquids: A Comparative Study

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Article info

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Highlights

- A comprehensive transient 2D model was developed to predict CO_2 capture via three ionic liquids in the membrane contactor.
- The results indicated good agreement between experimental and modeled CO₂ removal efficiency.
- The results indicated that emim[C₂N₂] gives the best efficiency and the longest lifetime.
- The model evaluated the effect of various input parameters on CO₂ capture efficiency.



Membrane

Abstract

The ability of technology and active solvents to absorb carbon dioxide from natural gas and after-combustion gases and to regenerate used solvents is a key representative of the search for efficient methods and environmentally friendly solvents. This study aims to construct a 2D model to evaluate the effectiveness of a hollow fiber membrane contactor (HFMC), in capturing CO_2 using three distinct types of ionic liquids (ILs): 1-butyl-3-methylimidazoliumtriflate (bmim [Triflate]), 1-Ethyl-3-methylimidazolium ethyl sulfate (emim[EtSO₄]), and 1-Ethyl-3-methylimidazolium dicyanamide (emim[C_2N_2]). The present model considers the storage tank for the solvent and considers its availability over time. By comparing the model predictions with experimental data, the results were in good agreement, with a slight discrepancy in the starting time for CO_2 uptake due to a time lag. Among the ILs evaluated, emim [C_2N_2] performs the best. Through sensitivity analysis, results reveal that increasing the feed flow rate and CO_2 partial pressure enhances both the CO_2 removal rate and prolongs solvent life.

1. Introduction

Extensive burning of fossil fuels and human activities significantly increases CO_2 emissions in the atmosphere and hence contributes to climate change and consecutive global warming. Accordingly, the reduction of these emissions is crucial and requires developing effective CO_2 removal strategies. [1,2]. An effective CO_2 capture technology is essential before it is released into the atmosphere. By doing this, we can reduce greenhouse gas releases and moderate the negative effects of climate change. The selected CO_2 capture technology should be energy-efficient, sustainable, cost-effective,

and environmentally friendly [3]. Such technologies are crucial for achieving the goals of global climate and maintaining a sustainable future for our planet. Among these capture technologies are the gas-liquid absorption column and membrane contacting processes [4]. In these technologies the selection of the appropriate solvent is important. The solvent should have a high selectivity for CO_2 capture (i.e., can remove a lot of CO_2 from the gas stream), be cost-effective, environmentally friendly, and be easy to regenerate (low energy consumption) [5]. Salt solutions of amino acids such as potassium threonate,

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potassium lysinate, and potassium sarcosinate were used for reducing CO_2 emissions [6].

Ionic liquids (ILs) made of ions instead of molecules are believed to have several advantages over conventional liquid solvents such as alkanolamine solvents. The IL solvent has low volatility (does not evaporate quickly, which prevents the IL from being lost to the atmosphere) and negligible vapor pressure (does not condense easily) that makes them identical to CO₂ capture and prevents them from clogging the membrane pores. Amino acids-based ionic liquids (Cholinium lysinate) were found to be effective absorbents for CO₂ separation from the gaseous mixture using 2D simulation in a hollow fiber membrane contactor [7]. ILs are stable over a wide range of temperatures, none toxic nor flammable [8-15]. CO₂ capture using membrane contactors has emerged as a promising approach to addressing the challenges of reducing greenhouse gas emissions [16]. These innovative devices utilize specialized membranes to selectively separate CO₂ from gas streams, offering significant advantages such as high efficiency, low energy consumption, and compact design. The membrane contactor technology facilitates the transfer of CO₂ across the membrane, enabling its capture while allowing other gases to pass through. This process not only helps mitigate the environmental impact of CO2 emissions but also presents opportunities for carbon capture and utilization. The application of membrane contactors for CO2 capture represents a valuable strategy in the pursuit of sustainable and eco-friendly solutions to combat climate change. A potential and promising technology for CO2 capture is the hollow fiber membrane contactors (HFMCs) that are composed of a bundle of polymeric or ceramic porous hollow fiber membranes located in a case, arranged like a shell and tube heat exchange. The gas stream flows in the tube side with solvent flows in the shell side or vice versa, in a concurrent or counter-current mode of operation. When the CO2 and solvent come into direct contact, CO2 dissolves in IL liquid which is later generated and used again (Fig. 1). Compared with traditional CO2 capture methods, HFMCs have several advantages such as high selectivity, low energy consumption, high mass transfer rates, and ease of scale-up [17-23]

The use of HFMCs along with ILs is a promising innovative technology that improved the efficiency of CO_2 absorption significantly. Several types of ILs exist among those are 1-butyl-3-methylimidazolium trifluoro-methane-sulfonate ([bmim][Triflate]), 1-ethyl-3-methylimidazolium ethyl sulfate ([emim][EtSO₄]), and 1-ethyl-3-methylimidazolium dicyanamide ([emim][DCA]), many others are under development and extensive research work is needed to develop ILs that are more cost-effective and environmentally friendly [24–26].

In this study and to the best of the author's knowledge a transient mathematical model was developed for the first time that includes the solvent storage tank and the ionic liquid circulation rate to investigate the potential use of various ILs solvents in HFMCs. Thus, the primary objective is to create a transient 2D mathematical model that can anticipate the point at which the solvents' recirculation becomes inactive and necessitates regeneration. Additionally, a thorough examination of different operating parameters was conducted.



Fig. 1. Schematic diagram describes solvent flowing in the membrane shell, while gas mixtures containing 15% CO₂/N₂ flow in the membrane shell.

2. Model development

Several assumptions were made to develop the mathematical model for CO_2 capture using IL systems in HFMCs. The system was assumed to be isothermal. The mass transfer of CO_2 between the gas and liquid phases was assumed to be governed by Henry's law and was described using a mass transfer coefficient [27]. The model also accounted for the transport of IL

through the HFMCs and the selective membrane coating the fibers. The mass balance equations were developed for the gas and liquid phases, which describe the concentration changes of CO₂, IL in the system over time. The equations were solved using numerical methods, and the simulation results were used to evaluate the performance of the IL in HFMCs under various operating conditions. The model development was based on a thorough review of the existing literature on ILs, and HFMCs. The model was validated using experimental data from previous studies, and the simulation results were found to be in good agreement with the experimental data. The overall mass transfer equation will be as follows [28]:

$$\frac{\partial C_i}{\partial t} = D_i \nabla^2 C_i - \nabla C_i V_z + R_i \tag{1}$$

where D_i , is the diffusion coefficient, V_z , is the axial velocity along the membrane module length. The reaction rate is R_i .

Equation (1) represents the component material balance within the tube ($C_{i,t}$) considering the convective term, diffusion term (with diffusion coefficient $D_{i,t}$), and reaction terms (R_i). This is founded upon the assumption of a steady-state condition. The initial point for the convective term is the velocity on the tube side ($V_{z,t}$), while the diffusion term originates from the diffusion coefficient ($D_{i,t}$) [29].

$$D_{i,t}\left(\frac{\partial^2 C_{i,t}}{\partial r^2} + \frac{1}{r}\frac{\partial C_{i,t}}{\partial r} + \frac{\partial^2 C_{i,t}}{\partial z^2}\right) - V_{z,t}\frac{\partial C_{i,t}}{\partial z} + R_{i,t} = \frac{dC_{i,t}}{dt}$$
(2)

The velocity profile on the tube side is represented by a parabola using the average velocity (V_{av}) and the ratio of the variable radius (r) to the inner radius of the inner tube (r_1). This relationship is illustrated by the following equation. The diffusivity in the tube side (gas) can be estimated using the following equation[30].

$$D_{CO_{2},g} = \frac{\left(0.01013T^{1.5} \left(\frac{1}{M_{w,CO_{2}}} + \frac{1}{M_{w,N_{2}}}\right)\right)}{P\left[(\Sigma v_{CO_{2}})^{\frac{1}{3}} (\Sigma v_{CO_{2}})^{\frac{1}{3}}\right]}$$
(3)

where, T(K) is the temperature, P(Pa) is the pressure, Mw(g/mol) is the molecular weight, and v is the atomic diffusion volume. The Navier-Stocks equation is also applied, revealing notable variations in the velocity profile. The velocity profile inside the hollow fiber ($V_{z,t}$) is described by the parabola [31,32].

$$V_{z,t} = 2v_a \left[1 - \left(\frac{r}{r_1}\right)^2 \right] \tag{4}$$

where, v_a is the average velocity, r_1 the membrane's inner radius. In the membrane segment, the pores of the membrane are filled with solvents because we assume the wetted mode. Diffusion begins with a parameter called $D_{i,m}$, and the only equations that control the process are related to the reactions taking place. We ignore the convective term. As a result, the concentration profile inside the membrane pores ($C_{i,m}$) reflects the balance of the material components in the following manner [33].

$$D_{i,m}\left(\frac{\partial^2 C_{i,m}}{\partial r^2} + \frac{1}{r}\frac{\partial C_{i,m}}{\partial r} + \frac{\partial^2 C_{i,m}}{\partial z^2}\right) = \frac{dC_{i,m}}{dt}$$
(5)

When the solvent is present on the tube side and gas on the shell side, and the membrane is dry (not wetted), the diffusion coefficient of CO₂ in the pores of the membrane ($D_{i,m}$) is influenced by three factors: the porosity (ϵ) and tortuosity (τ) of the porous membrane, as well as the diffusion of the component in the shell side ($D_{i,s}$).

$$D_{i,m} = \left[D_{i,s} \times \frac{\epsilon}{\tau} \right] \tag{6}$$

The distribution pattern of carbon dioxide ($C_{i,s}$) in the outer layer is described by the shell-side diffusion coefficient of CO₂ ($D_{i,s}$) and the velocity profile on the outer layer ($V_{z,s}$). There is no chemical reaction happening on this side, except within the falling film [34].

$$D_{i,s}\left(\frac{\partial^2 C_{i,s}}{\partial r^2} + \frac{1}{r}\frac{\partial C_{i,s}}{\partial r} + \frac{\partial^2 C_{i,s}}{\partial z^2}\right) - V_{z,s}\frac{\partial C_{i,s}}{\partial z} = \frac{dC_{i,s}}{dt}$$
(7)

The Navier-Stokes equations govern the movement of fluids and can be seen as an extension of Newton's second law of motion specifically designed for liquids. In the case of a compressible Newtonian fluid, the equations yield the following outcomes [29]:

$$\rho\left(\frac{\partial u}{\partial t} + u \cdot \nabla u\right) = -\nabla p + \nabla \cdot \left(\mu\left(\nabla u + \left(\nabla u\right)^T\right) - \frac{2}{3}\mu\left(\nabla \cdot u\right)I\right) + F \qquad (8)$$

where "u" represents the velocity of the fluid, "p" represents the pressure of the fluid, " ρ " represents the density of the fluid, and " μ " represents the fluid's dynamic viscosity.

The diffusivity of CO₂ in ionic liquid ($D_{CO_2,il}$) is influenced by the solvent viscosity (μ) and CO₂ molar volume (v_{CO_2})[35].

$$D_{CO_2,il}(cm^2.s^{-1}) = 2.66 \times 10^3 \mu^{-0.66} v_{CO_2}^{-1.04}$$
(9)

The individual terms correspond to the forces exerted on the fluid, including inertial, pressure, viscous, and external forces. Model development utilizes the parameters listed in Table 1. The comparison of the physical properties of the three solvents is listed in Table 2.

Table 3 presents the physical and chemical characteristics employed in the modeling process.

Table 1

Ceramic membrane speciation and feed conditions [36].

Parameters	value
Module length (cm)	11.5
Hollow fiber inner radius (mm)	0.11
Hollow fiber outer radius (mm)	0.15
Membrane pore diameter (um)	0.04
Module packing factor	0.39
Porosity	0.4
Inlet concentration of CO ₂ (vol%)	15
Liquid feed rate (ml/min)	50-90
Gas feed rate (ml/min)	50-100

Table 2

Physical properties of three different solvents (303K).

	bmim[triflate]	emim [EtSO ₄]	emim[C ₂ N ₃]	Ref.
Molecular weight (g/mol)	288.29	236.27	177.21	[37]
Density (g/cm ³)	1.12	1.237	1.108	[38-40]
Viscosity (mPa·s)	100	123.5	80	[41]

The porosity of a hollow fiber ceramic membrane may differ based on the membrane and its intended application. Nonetheless, typically, the porosity of a hollow fiber ceramic membrane can span approximately 30% or higher to 50% [42]. he density (ρ) and viscosity (μ) of [emim][EtSO₄] as a function of temperature [43].

$$\rho\left(\frac{g}{cm^3}\right) = 1.2541 - 5.98 \times 10^{-4} \left(T\left(K\right) - 273.15\right) \tag{10}$$

$$\mu(mPa.s) = 5.68 \times 10^{-3} T(K)^{0.5} \exp\left(\frac{945}{T(K) - 162}\right)$$
(11)

The Henry law solubility constant (H_k) of [emim][EtSO₄] as a function of temperature at moderate pressure is described by the following correlation [44].

$$H_k(Pa) = \exp(1.2492 + 0.005949T(K) - 1100 / T(K))$$
(12)

The distribution factor of CO₂ is influenced by the density of the ionic liquid $\rho(kg m^{-3})$, the ideal gas constant $R(8.314 J mol^{-1}K^{-1})$, the temperature T(K), Henry law solubility constant for CO₂ in ionic liquid $H_k(Pa)$, and the molecular weight of the ionic liquid (M_w) [45].

$$m = \rho RT / M_w H_k \tag{13}$$

Henry's constant, at moderate pressure (H_k) states that the solubility of a gas in a liquid is directly proportional to the partial pressure of the gas above the liquid. In other words, as the temperature increases, the solubility of gases in liquids generally decreases. The kinetic theory of gases can explain the relationship between Henry's law of solubility and temperature. According to this theory, as the temperature rises, the kinetic energy of gas molecules increases, leading to more rapid and energetic motion. This increased molecular motion reduces the ability of gas molecules to interact and become trapped within the liquid phase, resulting in lower solubility. Conversely, when the temperature decreases, the kinetic energy of gas molecules decreases, causing them to move more slowly. This slower movement allows gas molecules to interact and dissolve more readily in the liquid, resulting in higher solubility. Overall, Henry's law solubility is inversely affected by temperature, with higher temperatures generally leading to lower solubilities and lower temperatures leading to higher solubilities.

Table 3 Physical and chemical preparties used in modeling and simulation

Parameters	value	Reference
$D_{CO_2,g}\left(m^2.s^{-1}\right)$	1.55×10^{-5}	[35]
$V_{CO_2}\left(cm^3 / mol\right)$	34	[46]
$D_{CO_2,m}\left(m^2.s^{-1}\right)$	$D_{CO_2,g}(\epsilon / \tau)$	[47]
$D_{CO_2,il} (cm^2.s^{-1})$	$2.66 \times 10^3 \mu^{-0.66} v_{CO_2}^{-1.04}$	[48]
Porosity (ϵ)	0.40	[49]
Tortuosity (τ)	$(2-\epsilon)^2 / \epsilon$	[50]

The COMSOL Multiphysics version 6.1 software program was employed to develop a model for transporting CO_2 through a tube side, dry membrane, and shell side. The model utilized a Cartesian coordinate system to predict the CO_2 concentration at various locations within the system. We have employed structured multi-block grids to mesh the system to ensure high accuracy in the calculation and account for the flow field characteristics [51]. The liquid film region, where the flow phenomenon is complex, and the concentration gradient is the largest, is meshed most densely. In contrast, the shell side region experiences a more straightforward flow phenomenon with small velocity changes and is meshed less densely. The resulting mesh, as shown in Fig. 2, comprises 55,000 elements. This information is shown in Fig. 2, which presumably provides a visual representation of the meshing scheme.



Fig. 2. Optimal mesh generation for the four domains (tube, membrane, shell, and ILs tank) of hollow fiber membrane contactor using COMSOL Multiphysics 6.1.



Fig. 3. Mesh Refinement convergence graph - mesh elements vs. of the CO₂ relative concentration, gas feed rate 50 ml/min, the liquid feed rate is 60 ml/min, and the temperature is 300 K.

Fig. 3 presents the mesh analysis method to simulate and compute the CO_2 removal fraction in a hollow fiber membrane contactor. The plot in Fig. 3 shows how varying mesh density (number of elements) affects the mesh convergence and CO_2 exit concentration. The concentration of CO_2 in the exit stream of a reactor varied with the number of elements in the mesh until it reached a mesh number of around 35,000. Beyond this point, further refinement in the mesh did not significantly change the CO_2 concentration in the exit stream.

3. Results and discussion

3.1. Model validation

Fig. 4 shows the breakthrough curve of the dimensionless exit concentration of CO_2 from the tube side, increasing with time until CO_2 emerges from the membrane lumen side without being absorbed can be justified by the solvent saturation. As the CO_2 -containing feed gas passes through the tubular membrane system, the solvent initially exhibits a high absorption capacity, gradually increasing the exit concentration. However, as the solvent becomes saturated, it reaches its maximum capacity to absorb CO_2 , resulting in a plateau in the breakthrough curve. This is attributed to mass transfer and solubility limitations, where the ability of the ionic liquid solvent to absorb more CO_2 declines. The breakthrough profile indicates the need to regenerate the solvent, add fresh solvent, or use an alternative high absorption capacity solvent [26,53].

Fig. 5 shows the relative concentration of CO_2 when the solvent circulation rate is 60 ml/min, and the gas feed rate is 50 ml/min. Initially, there was a discrepancy between the model predictions and experimental data due to system instability and the possible time lag between the membrane module and gas analyzer [54]. However, after 30 minutes, the concentration profile fully developed and there was good agreement between simulation results and experimental data. Initially, for the first 3 min, the system

exhibited almost full removal of CO_2 , almost an efficiency of 100% for the initial recirculation rates of 60 ml/min, and gas feed rates of 50 ml/min. This high efficiency was measured by successfully removing CO_2 from the gas side. However, as recirculation continued, the system's efficiency gradually decreased [55].



Fig. 4. Comparison of current model prediction and experimental data for CO₂ absorption [52] with operation time at fixed IL circulation rate (60 ml/min) and gas feed rate (100 ml/min), and 15% CO₂ balance is N₂.



Fig. 5. Model validation, CO_2 average dimensionless concentration versus time under dry membrane mode, liquid circulation rate is 60 ml/min, and the gas feed rate is 50 ml/min.

3.2. Effect of diverse types of ionic liquids

The choice of diverse types of ionic liquids can have a significant effect on CO₂ absorption processes. Ionic liquids are a diverse class of compounds with various chemical structures and properties, which can influence their performance as solvents for CO₂ absorption. Different ionic liquids can exhibit varying degrees of solubility for CO₂. The selectivity of an ionic liquid refers to its ability to preferentially absorb CO2 over other gases present in a gas mixture. Ionic liquids can vary in viscosity, affecting their fluid dynamics and mass transfer properties. Higher viscosities may hinder the mass transfer of CO₂ between the gas and liquid phases, leading to slower absorption rates. Overall, the selection of diverse types of ionic liquids allows for the optimization of CO₂ absorption processes by tailoring the solubility, selectivity, viscosity, stability, and environmental impact to the specific requirements and objectives of the application. Fig. 6 displays the change in the tube gas dimensionless exit concentration with time for three diverse types of ionic liquids: bmim [Triflate], emim [EtSO₄], and emim[C₂N₂]. It is observed that, at a fixed time, the exit dimensionless concentration of bmim [Triflate] is greater than that of emim $[EtSO_4]$ and $emim[C_2N_2]$. This discrepancy suggests that emim[C2N2] exhibits a higher potential for absorbing more CO₂ than the other two ionic liquids. This finding can be attributed to the lower molecular weight of emim[C2N2] compared to the other two, which positively influences the distribution factor.



Fig. 6. Tube side exit dimensionless concentrations versus time for various ionic liquids. Solvent flow rate 60 ml/min, gas feed rate 50 ml/min.

Upon comparing the three ionic liquids, it becomes apparent that bmim [Triflate] exhibits the highest relative concentration compared to the other two. This signifies the poorer CO₂ capture capacity and absorption capability. Conversely, emim[C₂N₂] demonstrates a relatively lower exit dimensionless concentration compared to bmim [Triflate], followed by emim [EtSO₄]. This suggests that emim[C₂N₂] exhibits a stronger CO₂ absorption capacity than emim [EtSO₄]. The molecular weight of the ionic liquids plays a crucial role in their CO₂ absorption capabilities. In this instance, emim[C₂N₂] possesses a lower molecular weight than bmim [Triflate] and emim [EtSO4]. This lower molecular weight enhances CO₂ solubility and interaction, leading to a higher distribution factor. The distribution factor denotes an ionic liquid's ability to distribute and absorb more CO₂ within its structure.

3.3. Effect of temperature

Fig. 7 presents the impact of temperature on the relative CO_2 concentration in the membrane tube side with operation time. The results revealed that, as the temperature increases the amount of CO_2 absorbed drops and accordingly the relative concentration increases. That is attributed to the decrease in the CO_2 distribution factor with temperature increases (eq (12)). The distribution factor is directly proportional to the operating temperature and inversely relative to Henry's constant of CO_2 at zero pressure in the investigated ionic liquids. It looks that Henry's constant has a dominant influence on the distribution factor as it increases with temperature increases [44]. The CO_2 solubility in ILs decrease with temperature increases. The reduced viscosity influences the mass transfer characteristics of the system.



Fig. 7. On the tube side, CO₂ relative concentrations versus time at various temperatures. Liquid flow rate 60 ml/min, gas feed rate 50 ml/min.

3.4. Effect of storage tank size

The size of the storage tank for an ionic liquid can impact the circulation rate in CO₂ absorption processes, but it is not a direct or primary factor. The critical role of the storage tank is to provide an adequate supply of ionic liquid for the absorption process rather than directly influencing the circulation rate. The size of the storage tank can indirectly influence the circulation rate by providing a sufficient volume of ionic liquid to maintain the desired flow rate over a specific duration. A larger storage tank may allow for longer continuous operation or accommodate higher circulation rates without frequent refills. Fig. 8 presents the circulation profile of the solvent. It shows the path of the solvent as it enters the upper section of the membrane shell side and exits through the other side into the tank. These specific values enable researchers to assess the system's behavior under controlled conditions and draw meaningful conclusions regarding its functionality and potential improvements. Fig. 8 illustrates the relative outlet concentrations of CO₂ in the complete membrane module and the ionic liquid storage tank following 20 minutes of operation. The ionic liquid circulation rate was 60 ml/min, while the gas feed rate was 50 ml/min. The figures show the concentration flux profile.



Fig. 8. Tube side CO_2 relative concentrations versus time at various ionic liquid storage tank sizes. Liquid flow rate 60 ml/min, gas feed rate 50 ml/min, temperature 300K.

3.5. Effect of gas feed rate

In the present HFMC configuration, the gas flows in the tube side and the IL flows in the shell side counter-currently. Fig. 9a presents the influence of gas feed rate on the relative CO₂ concentration. As the gas feed rate increases, the relative CO₂ concentration increases which means the percentage of the removal efficiency decreases. The phenomenon is attributed to decreasing residence time with increasing the gas feed rate. In other words, it decreases gas time spent in direct contact with the liquid solvent [56]. Fig. 9b is the enlargement zone of Fig. 9a for the CO₂ absorption before 20 min of operation. Fig. 9b reveals that complete separation was observed initially for a period below approximately 4 minutes of operation. The separation drops sharply between 4 and 10 min and then maintains the reactive concentration between 10 to 20 min. that is attributed to the sufficient available amount of solvent to absorb CO2. The absorption gradually dropped after 20 min. Initially, the high removal efficiency is attributed to fully functional fresh liquid and contactor. The sharp increase in the relative concentration (i.e., drop in the removal efficiency) is attributable to the concentration polarization that may occur when the CO2 concentration near the membrane surface becomes significantly lower than in the bulk of the gas stream. The diffusion resistance created due to this concentration gradient slows the mass transfer of CO₂ from the gas to the ionic liquid which leads to a reduction in the CO2 removal efficiency. The removal efficiency stabilization between 10 and 20 min. occurs because the dynamical equilibrium is reached between the concentration polarization effects and the rate of mass transfer, resulting in a relatively constant removal efficiency for a certain period. The continuous drop after 20 min of operation is attributed to the saturation of the ionic liquids and can come into play. To maintain higher and more consistent removal efficiency, solvent regeneration or selecting an ionic liquid with higher CO₂ affinity [57-59].



Fig. 9. (a)Tube side, CO₂ relative concentrations profile versus time at various inlet gas flow rates and constant liquid flow rates (60 ml/min), and fixed temperature (300 K) (b) Enlargement of the zone before 20 min.



Fig. 10. (a) Tube side, CO₂ relative concentrations profile versus time at various ionic liquid circulation rates at a constant gas flow rate (100 ml/min) and temperature (300 K) (b) enlargement of the zone within 20 min.

3.6. Effect of ionic liquid circulation rate

The effect of ionic liquid circulation rate on the relative CO_2 concentration in the tube side of a hollow fiber membrane contactor can vary depending on the specific system and operating conditions (Fig. 10a has been enlarged in Fig. 10b). Increasing the ionic liquid circulation rate on the shell side of the contactor can enhance the mass transfer rate of CO_2 across the membrane [52]. This is because a higher flow rate can help maintain a concentration gradient across the membrane, facilitating the transfer of CO_2 from the tube side to the shell side. The circulation rate affects the residence time of the ionic liquid in the contactor. A higher circulation rate typically leads to a shorter residence time, meaning the ionic liquid spends less time in contact with the membrane. This can limit the opportunity for CO_2 to permeate through the membrane, potentially reducing the CO_2 concentration on the tube side [60,61].

3.7. Total flux profile

The change in CO₂ total flux with time refers to how the total amount of carbon dioxide (CO₂) transported or transferred through a system or medium varies over a specific period. Factors such as concentration gradients, diffusion rates, and transport mechanisms can influence CO2 total flux, and the flux can change over time due to alterations in these factors or system conditions [62]. On the other hand, modeling techniques use mathematical equations and computational simulations to predict the behavior of CO₂ flux over time. These models consider factors such as concentration gradients, diffusion coefficients, and transport properties to simulate the change in flux. The change in CO₂ total flux with time can provide valuable insights into the dynamics of CO₂ transport and the efficiency of systems or processes involved in CO₂ capture, storage, or transport (Fig. 11). It helps understand how the flux evolves and allows for optimizing and improving CO2 management strategies. With time, more CO_2 is absorbed; hence, the CO_2 concentration in the ionic liquid circulation region tank increases (Fig. 11). Both Fig. 11 and Fig. 12 work in tandem to depict the concentration flux profile, providing a visual representation of how the CO₂ concentrations vary across different system components.



Fig. 11. CO_2 surface concentrations of CO_2 in the complete membrane module and the ionic liquid storage tank following 10 minutes of operation. The ionic liquid circulation rate was 60 ml/min, while the gas feed rate was 50 ml/min.



Fig. 12. CO_2 surface concentrations of CO_2 in the complete membrane module and the ionic liquid storage tank following 20 minutes of operation. The ionic liquid circulation rate was 60 ml/min, while the gas feed rate was 50 ml/min.

4. Conclusion

This paper presents a novel 2D transient mathematical model that includes the storage tank to simulate CO2 capture using three different ionic liquids (ILs) systems in hollow fiber membrane contactors (HFMCs) while considering the circulation of the IL. The simulation results demonstrate the potential of IL-HFMCs as an efficient approach for CO₂ capture, leading to reduced energy consumption and a more favorable environmental footprint. The results indicate that the efficiency of CO₂ capture improves as the feed flow rate and CO₂ partial pressure increase. Moreover, the transient simulation results suggest that the utilization of IL systems in HFMCs significantly enhances the CO₂ capture efficiency compared to other solvents. This article aims to model an approach that significantly contributes to enhancing our understanding of CO2 mass transfer in HFMCs, enabling the improvement of HFMC design and operation for the development of more effective and economically viable CO2 capture technologies. In summary, IL-HFMCs exhibit improved CO2 capture efficiency with higher feed flow rates and CO₂ partial pressures, and the modeling presented in this article provides valuable insights into CO2 mass transfer in HFMCs.

Nomenclature

C_i	the molar concentration of component ' i "(mol/m ³)
D_i	diffusion coefficient (m ² /s)
$D_{CO_2,g}$	diffusion coefficient of CO_2 in the gas phase (m ² /s)
$D_{CO_2,il}$	diffusion coefficient of CO_2 in ionic liquid (m ² /s)
$D_{CO_2,m}$	diffusion coefficient of CO_2 in membrane skin (m ² /s)
H_k	Henry's law solubility constant for CO ₂ (Pa)
$M_{\mu\nu}$	the molecular weight of the ionic liquid (g/mol)
P	the pressure of the fluid (atm)
R	Ideal gas constant $\left(8.314 J mol^{-1} K^{-1}\right)$
R _i	the reaction rate (mol/m ³ .s)
r	variable radius (m)
r _l	inner tube radius (m)
r_2	outer tube radius (m)
T	the temperature (K)
V _{av}	average velocity (m/s)
V_{CO_2}	CO ₂ molar volume (34 cm ³ /mol)
V_z	the axial velocity along the membrane module length
	(m/s)
Greek symbols	
ϵ	membrane porosity
τ	tortuosity
ρ	density of the fluid (kg/m ³)
11	fluid's dynamic viscosity (Pa.s)

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Data availability

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CRedit authorship contribution statement

N. Ghasem: Conceptualization; Data curation; Formal analysis; Funding acquisition; Investigation; Methodology; Project administration; Resources; Software; Supervision; Validation; Visualization; Writing - original draft; Writing - review & editing.

Declaration of Competing Interest

The author declares that he has no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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